

Van Horne Chapter 4. The Valuation of Long-Term Securities (continued)

**Non-Zero Coupon Paying Bond**

A non-zero coupon-paying bond is a coupon paying bond with a finite life.

$$V = I (PVIFA_{kd, n}) + MV (PVIF_{kd, n}) \text{ or } V = PV (\text{Interest Payments}) + PV (MV)$$

PVIF = present value interest factor

V = value; I = interest payment; MV = maturity value

kd = discount rate; n = number of periods

**Example 4.14.** Bond C has a \$1,000 face value and provides an 8% annual coupon for 30 years. The appropriate discount rate is 10%. What is the value of the *coupon bond*?

1. Calculate the annual coupon payment:  $\$1000 * .08$ . **\$80**
2. Find the PV of an \$80 annuity for 30 periods at 10%. **\$754.16**
3. Find the PV of a bond with a MV of \$1000 in 30 periods discounted at 10%. **\$57.00**
4. Add the two PVs: **\$754.16 + \$57.00 = \$811.16**

**Zero-Coupon Bond**

A **zero-coupon bond** is a bond that pays no interest but sells at a deep discount from its face value; it provides compensation to investors in the form of price appreciation.

**Example 4.17.** Bond Z has a \$1,000 face value and a 30-year life. The appropriate discount rate is 10%. What is the value of the *zero-coupon bond*?

1. Find the PV of a bond with a MV of \$1000 in 30 years discounted at 10%. **\$57.00**

**Semiannual Coupon Bond**

Most bonds in the US pay interest twice a year (1/2 of the annual coupon).

**Example 4.21.** Bond C has a \$1,000 face value and provides an 8% semi-annual coupon for 15 years. The appropriate discount rate is 10% (annual rate). What is the value of the *coupon bond*?

1. Calculate the annual coupon payment:  $\$1000 * .08$ . **\$80**
2. Divide the annual payment and discount rate by 2: **\$40, 5%**
3. Find the PV of an \$40 annuity for 30 periods at 5%. **\$614.92**
4. Find the PV of a bond with a MV of \$1000 in 30 periods discounted at 5%. **\$231.00**
5. Add the two PVs: **\$614.92 + \$231.00 = \$845.92**

**Preferred Stock**

Preferred Stock is a type of stock that promises a (usually) fixed dividend, but at the discretion of the board of directors. Preferred Stock has preference over common stock in the payment of dividends and claims on assets.

**Example 4.28.** Stock PS has an 8%, \$100 par value issue outstanding. The appropriate discount rate is 10%. What is the value of the preferred stock?

Dividend =  $Div_P = \$100 ( 8\% ) = \$8.00$ . Discount rate of the preferred stock =  $k_P = 10\%$ .

Value =  $V = Div_P / k_P = \$8.00 / 10\% = \$80$

## Common Stock

Common stock represents a residual ownership position in the corporation.

- Pro rata share of future earnings after all other obligations of the firm (if any remain).
- Dividends *may* be paid out of the pro rata share of earnings.

What cash flows will a shareholder receive when owning shares of common stock?

- (1) Future dividends (PV of an annuity)
- (2) Future sale of the common stock shares (PV of a FV)

There are three stock growth models: constant growth, zero growth, and growth phase models.

### Constant Growth Model

The constant growth model assumes that dividends will grow forever at the rate  $g$ .

$$\frac{D_1}{k_e - g}$$

$D_1$ : Dividend paid at time 1.

$g$ : The constant growth rate.

$k_e$ : Investor's required return.

**Example 4.35.** Stock CG has an expected dividend growth rate of 8%. Each share of stock just received an annual \$3.24 dividend. The appropriate discount rate is 15%. What is the value of the common stock?

$$D_1 = \$3.24 (1 + 0.08) = \mathbf{\$3.50}$$

$$V_{CG} = D_1 / (k_e - g) = \$3.50 / (0.15 - 0.08) = \$3.50 / .07 = \mathbf{\$50}$$

### Zero Growth Model

The zero-growth model assumes that dividends will grow forever at the rate  $g = 0$ .

$$\frac{D_1}{k_e}$$

$D_1$ : Dividend paid at time 1.

$k_e$ : Investor's required return.

**Example 4.37.** Stock ZG has an expected growth rate of 0%. Each share of stock just received an annual \$3.24 dividend per share. The appropriate discount rate is 15%. What is the value of the common stock?

$$D_1 = \$3.24 (1 + 0) = \mathbf{\$3.24}$$

$$V_{ZG} = D_1 / (k_e - 0) = \$3.24 / (0.15 - 0) = \$3.24 / .15 = \mathbf{\$21.60}$$

### Growth Phases Model

The growth phases model assumes that dividends for each share will grow at two or more *different* growth rates.

Next Class